

LING/C SC 581:

Advanced Computational Linguistics

Lecture 10

Prof. Sandiway Fong

Today's Topic

- *Leaving the topic of context-sensitive languages*
- Turn to writing our own CFGs for natural language:
 1. A note on SWISH (SWI-Prolog for Sharing)
 2. *agreement* in natural language
 3. the problem with Prolog & left recursion
 4. a grammar transformation:
 - left recursive to right recursive **BUT** *structure preserving*
- *Homework 6 (note deadline change)*

SWISH = SWI Prolog for SHaring

The screenshot shows the SWISH web interface in a browser window. The address bar displays `swish.swi-prolog.org`. The page title is "SWISH -- SWI-Prolog for SHaring". The navigation bar includes "File", "Edit", "Examples", and "Help" menus, along with a search bar and a notification for "123 users online".

The main content area is split into two columns. The left column contains a "New tab" button, a "Create a" section with "Program" and "Notebook" buttons, and a search bar with the query `user:"me"`. Below the search bar, a red warning message states "No matching files" and provides instructions for new users.

The right column features a large, stylized owl logo. Below the logo is a text input field with the placeholder text "Your query goes here ...". At the bottom of the right column, there are buttons for "Examples", "History", and "Solutions", along with a "table results" checkbox and a "Run!" button.

SWISH <https://swish.swi-prolog.org>

```
:- use_rendering(svgtree, [list(false)]).
```

The screenshot displays the SWISH Prolog environment. On the left, a code editor shows a Prolog program with 10 lines of code. The main window shows the execution of the program, resulting in a parse tree for the sentence "the man kicked the ball". The parse tree is a binary tree with root node 's'. The left child of 's' is 'np', which has children 'dt' (the) and 'nn' (man). The right child of 's' is 'vp', which has children 'vbd' (kicked) and 'np'. The 'np' child of 'vp' has children 'dt' (the) and 'nn' (ball). Below the parse tree, the execution console shows the query `s(Parse, [the,man,kicked,the,ball], []).` and the result `s(Parse, [the,man,kicked,the,ball], []).`. On the right, a stack of frames is visible, showing the current frame `f(X,S,[]).` and several other frames with variables `S` and `X` bound to lists and integers.

```
1 :- use_rendering(svgtree, [list(false)]).
2 s(s(NP, VP)) --> np(NP), vp(VP).
3 np(np(DET, NN)) --> det(DET), nn(NN).
4 det(dt(the)) --> [the].
5 det(dt(a)) --> [a].
6 nn(nn(man)) --> [man].
7 nn(nn(ball)) --> [ball].
8 vp(vp(VTR, NP)) --> vtr(VTR), np(NP).
9 vtr(vbd(kick_ed)) --> [kicked].
10 vtr(vbd(hit_ed)) --> [hit].
```

Parse =

```
graph TD
    s[s] --- np1[np]
    s --- vp[vp]
    np1 --- dt1[dt]
    np1 --- nn1[nn]
    dt1 --- the1[the]
    nn1 --- man[man]
    vp --- vbd[vbd]
    vp --- np2[np]
    vbd --- kick[kick]
    vbd --- ed[ed]
    np2 --- dt2[dt]
    np2 --- nn2[nn]
    dt2 --- the2[the]
    nn2 --- ball[ball]
```

?- s(Parse, [the,man,kicked,the,ball], []).

Next 10 100 1,000 Stop

?- f(X,S,[]).

SWI-Tinker (*inside your browser*)

This is **SWI-Tinker**: **SWI-Prolog** running inside your browser
Please consult our [Wiki for help](#) Star 9

Welcome to SWI-Prolog (32 bits, version 10.1.0)
SWI-Prolog comes with ABSOLUTELY NO WARRANTY. This is free software.
Please run `?- license.` for legal details.

For online help and background, visit <https://www.swi-prolog.org>

```
?- use_rendering(svgtree, [list(false)]).
```

```
ERROR: [Thread main] Unhandled exception: toplevel: Unknown procedure: use_rendering/2 (DWIM could not correct goal)
```

```
?- 
```

```
?- consult('/prolog/scratch.pl').
```

```
ERROR: /prolog/scratch.pl:1:
ERROR:   catch/3: Unknown procedure: use_rendering/2
Warning: /prolog/scratch.pl:1:
Warning:   Goal (directive) failed: user:use_rendering(svgtree,[list(false)])
true.
```

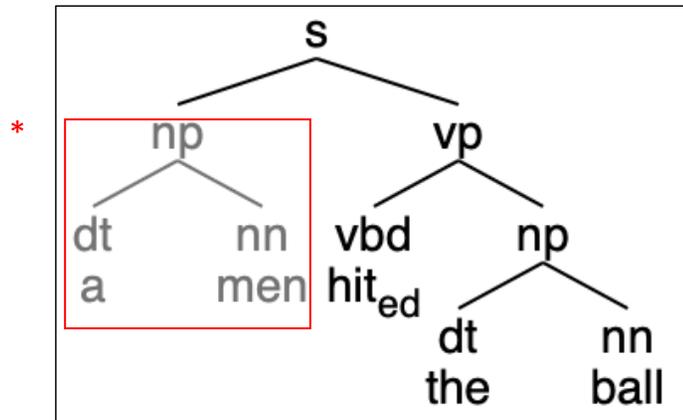
```
?- 
```

(Re)consult

Extra Arguments: Agreement

- **Idea:**

- We can also use an extra argument to impose constraints between constituents within a DCG rule



- **Example:**

- English number agreement between DT and NN
- Data:
 - the man the men
 - a man *a men
- Lexical Features (Number):
 - *man* value singular (sg)
 - *men* value plural (pl)
 - *the* value singular or plural (sg/pl)
 - *a* value singular (sg)

* means ***ungrammatical***

Recall a Class Exercise: agree/2

```

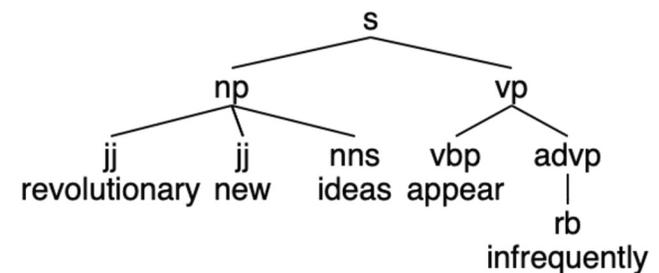
1 s(s(NP,VP)) --> np(NP,NUM), vp(VP,INFL), {agree(NUM,INFL)}.
2 np(np(JJ1,NNS),pl) --> jj(JJ1), nns(NNS).
3 np(np(JJ1,JJ2,NNS),pl) --> jj(JJ1), jj(JJ2), nns(NNS).
4 np(np(JJ1,JJ2,NN),sg) --> jj(JJ1), jj(JJ2), nn(NN).
5 np(np(JJ1,NN),sg) --> jj(JJ1), nn(NN).
6 vp(vp(VBP,ADVP), pres) --> vbp(VBP), advp(ADVP).
7 vp(vp(VBZ,ADVP), pres3sg) --> vbz(VBZ), advp(ADVP).
8 vp(vp(VBD,ADVP), past) --> vbd(VBD), advp(ADVP).
9 advp(advp(RB)) --> rb(RB).
10 jj(jj(Adj)) --> [Adj], {member(Adj,[colorless, green, revolutionary, new])}
11 nns(nns(NNS)) --> [NNS], {member(NNS,[ideas])}.
12 nn(nn(NN)) --> [NN], {member(NN,[idea])}.
13 vbp(vbp(VBP)) --> [VBP], {member(VBP,[sleep, appear])}.
14 vbz(vbz(VBZ)) --> [VBZ], {member(VBZ,[sleeps, appears])}.
15 vbd(vbd(VBD)) --> [VBD], {member(VBD,[slept, appeared])}.
16 rb(rb(RB)) --> [RB], {member(RB,[furiously, infrequently])}.
17
18 % agree(NUM,INFL).
19 agree(pl, pres).
20 agree(sg, pres3sg).
21 agree(_, past).

```

```

?-
s(P,[revolutionary,new,ideas,appear,infrequently],[]).
P = s(np(jj(revolutionary), jj(new), nns(ideas)),
vp(vbp(appear), advp(rb(infrequently)))) ;
false.

```



Determiner-Noun Agreement

- Example (n13.prolog):

1. np(np(DET, NN)) --> det(DET, NUM), nn(NN, NUM).
2. det(dt(the), sg) --> [the].
3. det(dt(the), pl) --> [the].
4. det(dt(a), sg) --> [a].
5. nn(nn(man), sg) --> [man].
6. nn(nn(men), pl) --> [men].
7. nn(nn(ball), sg) --> [ball].
8. vp(vp(VTR, NP)) --> vtr(VTR), np(NP).
9. vtr(vbd(kick_ed)) --> [kicked].
10. vtr(vbd(hit_ed)) --> [hit].

Extra Argument: Agreement

Note:

- extra argument NUM for agreement here is basically “syntactic sugar” and **lends no more expressive** power to the grammar rule system:
- *i.e. we can enforce agreement without the use of the extra argument at the cost of writing more rules*

- Instead of

```
np(np(DET, NN)) --> det(DET, NUM), nn(NN, NUM).
```

could have encoded NUM into the nonterminal name:

```
np(np(DET, NN)) --> det_sg(DET), nn_sg(NN).
```

```
np(np(DET, NN)) --> det_pl(DET), nn_pl(NN).
```

```
det_sg(dt(the)) --> [the].
```

```
det_pl(dt(the)) --> [the].
```

```
det_sg(dt(a)) --> [a].
```

```
nn_sg(nn(man)) --> [man].
```

```
nn_pl(nn(men)) --> [men].
```

```
nn_sg(nn(ball)) --> [ball].
```

nl4.prolog

Left recursion and Prolog DCGs

- **Aside:** *what is the language of this grammar?*
- `left.prolog`:
 1. `s --> x, y.`
 2. `x --> x, [a].`
 3. `x --> [a].`
 4. `y --> [b].`

Rule ordering

- Example (left.prolog):

1. `s --> x, y.`
2. `x --> x, [a].`
3. `x --> [a].`
4. `y --> [b].`

- An idea (swap rules 2 and 3):

1. `s --> x, y.`
2. `x --> [a].`
3. `x --> x, [a].`
4. `y --> [b].`

; eventually
calls for
stacking rule 3.
12 million deep

- (left2.prolog)

```
[?- [left2].  
true.  
[?- s([a,b], []).  
true
```

```
[?- s([a,b], []).  
true ;  
ERROR: Stack limit (1.0Gb) exceeded  
ERROR: Stack sizes: local: 1.0Gb, global: 25Kb, trail: 0Kb  
ERROR: Stack depth: 12,200,438, last-call: 0%, Choice points: 3  
ERROR: Probable infinite recursion (cycle):  
ERROR: [12,200,438] user:x([length:2], _6582)  
ERROR: [12,200,437] user:x([length:2], _6608)
```

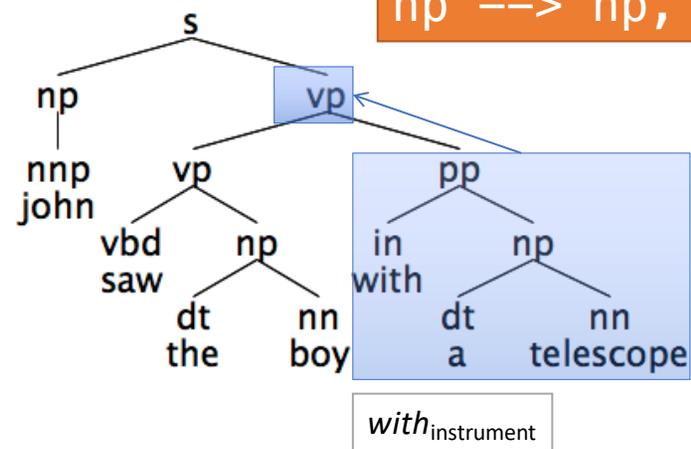
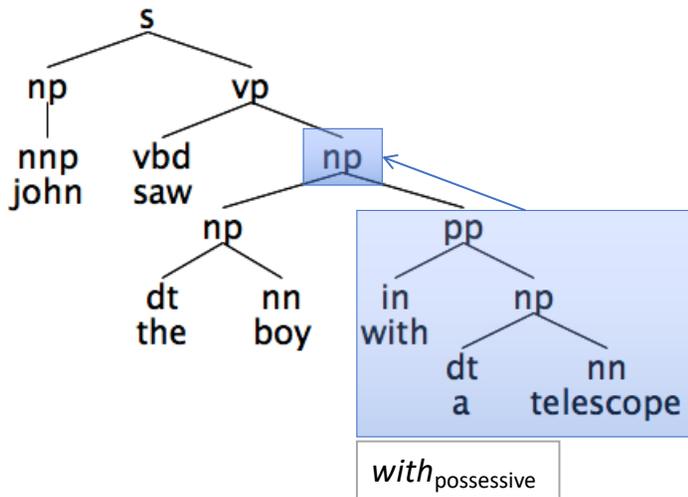
Big picture question

- Is this just a **theoretical problem**: i.e. not a problem for natural language grammars?
- **Unfortunately**, it is a problem ...
 - *John saw the boy with a telescope*
 - is **structurally ambiguous** wrt. attachment of the PP *with a telescope*
 - (PP = prepositional phrase)

Preposition Phrase (PP) Attachment

- The preferred syntactic analysis is a left recursive parse
- Example:
 - *John saw the boy with a telescope*

Rules are:
 vp \rightarrow vp, pp.
 np \rightarrow np, pp.



Preposition Phrase (PP) Attachment

<https://parser.kitaev.io>

Sentence:
John saw the boy with a telescope

Parse tree:

```

graph TD
    S --> NP1[NP]
    S --> VP[VP]
    NP1 --> NNP[NNP]
    NNP --> John[John]
    VP --> VBD[VBD]
    VBD --> saw[saw]
    VP --> NP2[NP]
    NP2 --> DT1[DT]
    DT1 --> the1[the]
    NP2 --> NN1[NN]
    NN1 --> boy[boy]
    VP --> PP[PP]
    PP --> IN[IN]
    IN --> with[with]
    PP --> NP3[NP]
    NP3 --> DT2[DT]
    DT2 --> a[a]
    NP3 --> NN2[NN]
    NN2 --> telescope[telescope]
  
```

Incorrect rule used:
vp --> vbd, np, pp.

<https://cloud.google.com/natural-language>

Dependency
 Parse label
 Part of speech
 Lemma
 Morphology

nsbj	root	det	dobj	prep	det	pobj
John	saw	the	boy	with	a	telescope
NOUN	VERB	DET	NOUN	ADP	DET	NOUN
number=SINGULAR	mood=INDICATIVE		number=SINGULAR			number=SINGULAR
proper=PROPER	tense=PAST					

dependency parse (essentially same problem):
 root is saw
 root --> prep
 root --> dobj.

Class Exercise

- Let's add PP-attachment rules mentioned earlier to `n13.prolog`
 - `vp --> vp, pp.`
 - `np --> np, pp.`
- Need to add:
 - verb (VBD): *saw – past tense (-ed)*
 - preposition (IN): *with*
 - singular nouns (NN): *telescope, boy, limp*
 - proper noun (NNP): *john ('John'), mary ('Mary')*
 - recall: *initial caps = Prolog variable*

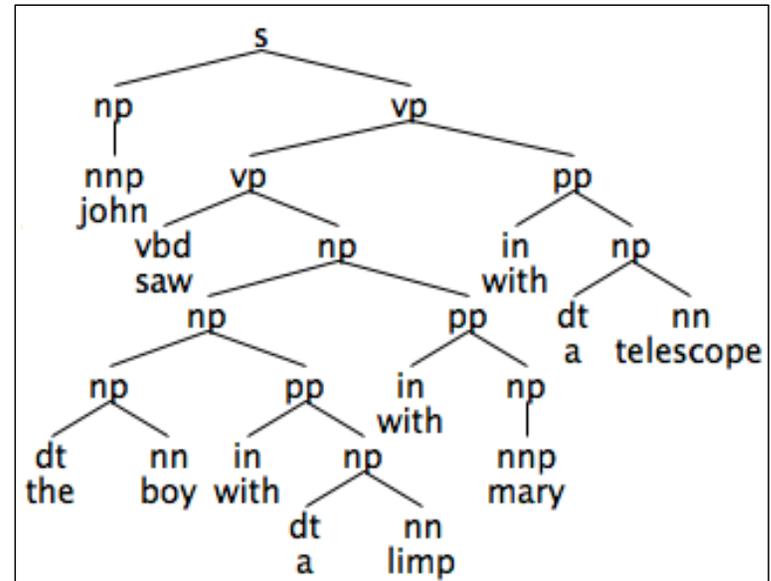
Penn Part-of-Speech (POS) Tagset

Tag	Description	Example	Tag	Description	Example	Tag	Description	Example
CC	coord. conj.	<i>and, but, or</i>	NNP	proper noun, sing.	<i>IBM</i>	TO	“to”	<i>to</i>
CD	cardinal number	<i>one, two</i>	NNPS	proper noun, plu.	<i>Carolinas</i>	UH	interjection	<i>ah, oops</i>
DT	determiner	<i>a, the</i>	NNS	noun, plural	<i>llamas</i>	VB	verb base	<i>eat</i>
EX	existential ‘there’	<i>there</i>	PDT	predeterminer	<i>all, both</i>	VBD	verb past tense	<i>ate</i>
FW	foreign word	<i>mea culpa</i>	POS	possessive ending	<i>'s</i>	VBG	verb gerund	<i>eating</i>
IN	preposition/ subordin-conj	<i>of, in, by</i>	PRP	personal pronoun	<i>I, you, he</i>	VBN	verb past partici- ple	<i>eaten</i>
JJ	adjective	<i>yellow</i>	PRP\$	possess. pronoun	<i>your, one's</i>	VBP	verb non-3sg-pr	<i>eat</i>
JJR	comparative adj	<i>bigger</i>	RB	adverb	<i>quickly</i>	VBZ	verb 3sg pres	<i>eats</i>
JJS	superlative adj	<i>wildest</i>	RBR	comparative adv	<i>faster</i>	WDT	wh-determ.	<i>which, that</i>
LS	list item marker	<i>1, 2, One</i>	RBS	superlatv. adv	<i>fastest</i>	WP	wh-pronoun	<i>what, who</i>
MD	modal	<i>can, should</i>	RP	particle	<i>up, off</i>	WP\$	wh-possess.	<i>whose</i>
NN	sing or mass noun	<i>llama</i>	SYM	symbol	<i>+, %, &</i>	WRB	wh-adverb	<i>how, where</i>

Figure 8.2 Penn Treebank part-of-speech tags.

Preposition Phrase (PP) Attachment

- The preferred syntactic analysis is a left recursive parse
 - notice PPs can be “stacked”, as in:
 - *John saw the boy with a limp with Mary with a telescope*
 - *with*-ambiguity:
 - *with*_{possessive}
 - *with*_{accompaniment}
 - *with*_{instrument}



Preposition Phrase Attachment

- Linguistically:
 - PP (recursively) adjoins to NP or VP
 - $\text{np}(\text{np}(\text{NP}, \text{PP})) \rightarrow \text{np}(\text{NP}), \text{pp}(\text{PP})$.
 - $\text{vp}(\text{vp}(\text{VP}, \text{PP})) \rightarrow \text{vp}(\text{VP}), \text{pp}(\text{PP})$.
- Left recursion gives Prolog problems
- Derivation (top-down, left-to-right):

1. vp
2. vp pp
3. vp pp pp
4. vp pp pp pp
5. vp pp pp pp pp

Note:

only the parse tree argument shown [here](#)
other extra arguments are possible

infinite loop...

Transformation

- Apply the general left to right recursive transformation:

$x(x(X,y)) \rightarrow x(X), [y].$
 $x(x(z)) \rightarrow [z].$



$x(X) \rightarrow [z], w(X,x(z)).$
 $x(x(z)) \rightarrow [z].$
 $w(W,X) \rightarrow [y], w(W,x(X,y)).$
 $w(x(X,y),X) \rightarrow [y].$

Note:
 w is a *fresh*
 nonterminal
 that takes 2
 arguments

- to the NP rules:

1. $\frac{np(np(DT,NN))}{x} \rightarrow dt(DT,Number), [z]nn(NN,Number).$

2. $\frac{np(np(NP,PP))}{x} \rightarrow \frac{np(NP)}{x}, \frac{pp(PP)}{[y]}.$

x is the recursive nonterminal

Transformation

• Consider input strings:

1. $[z]$
2. $[z, y]$
3. $[z, y_1, y_2]$

Parse:

- $x(z)$
- $x(x(z), y)$
- $x(x(x(z), y_1), y_2)$

Transformed rules:

- 2
- 1 + 4
- 1 + 3 + 4

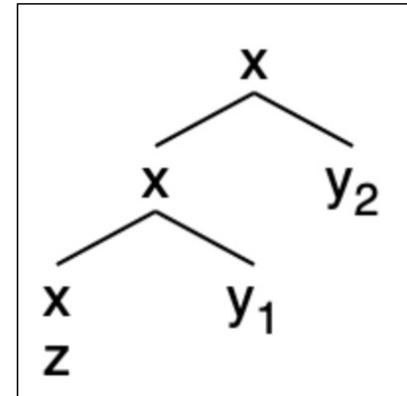
1. $x(x(X, y)) \rightarrow x(X), [y]$.
2. $x(x(z)) \rightarrow [z]$.



1. $x(X) \rightarrow [z], w(X, x(z))$.
2. $x(x(z)) \rightarrow [z]$.
3. $w(W, X) \rightarrow [y], w(W, x(X, y))$.
4. $w(x(X, y), X) \rightarrow [y]$.

Steps for example 3:

- $[z, \bullet y_1, y_2]$ rule 1: call nonterminal $w(X, x(z))$
- $[z, y_1, \bullet y_2]$ rule 3: call nonterminal $w(X, x(x(z), y_1))$
- $[z, y_1, y_2 \bullet]$ rule 4: answer $X = x(x(x(z), y_1), y_2)$



the left recursive structure formed by a right recursive parse of $[z, y_1, y_2]$

Homework 6

- Question 1: apply the transformation to the left recursion starting with `nl3.prolog`:
 - `np(np(NP,PP)) --> np(NP), pp(PP).`
 - `vp(vp(VP,PP)) --> vp(VP), pp(PP).`
- Show your grammar working properly on example sentences:
 1. the boy saw the man with the telescope
 2. the boy with the telescope saw the man
 3. the boy kicked the man with the telescope
 4. the boy with the telescope kicked the man
 5. the boy with the telescope kicked the man with the limp
- Show all possible parses (;) until **false** in each case

Homework 6

```

1 s(s(NP, VP)) --> np(NP), vp(VP).
2 np(np(DET, NN)) --> det(DET, NUM), nn(NN, NUM).
3
4

```

```

s(Parse,[the, boy, saw, the, man, with, the, telescope],[]).

```

```

Parse = s(
  np(dt(the),nn(boy)),
  vp(
    vbd(see_ed),np(dt(the),nn(man))),
    pp(in(with),np(dt(the),nn(telescope)))
  )
)

```

```

Parse = s(
  np(dt(the),nn(boy)),
  vp(
    vbd(see_ed),
    np(np(dt(the),nn(man)),pp(in(with),np(dt(the),nn(telescope))))
  )
)

```

false

No more parses! →

```

1 :- use_rendering(svgtree, [list(false)]).
2 s(s(NP, VP)) --> np(NP), vp(VP).
3 np(np(DET, NN))
4 % np(np(NP, PP))
5 % vp(vp(NP, PP))

```

```

s(Parse,[the, boy, saw, the, man, with, the, telescope],[]).

```

```

Parse =

```

```

graph TD
  s --> np1[np]
  s --> vp1[vp]
  np1 --> dt1[dt]
  np1 --> nn1[nn]
  dt1 --> the1[the]
  nn1 --> boy[boy]
  vp1 --> vbd[vbd]
  vp1 --> np2[np]
  vp1 --> pp[pp]
  vbd --> see[see]
  vbd --> ed[ed]
  np2 --> dt2[dt]
  np2 --> nn2[nn]
  dt2 --> the2[the]
  nn2 --> man[man]
  pp --> in[in]
  pp --> np3[np]
  in --> with[with]
  np3 --> dt3[dt]
  np3 --> nn3[nn]
  dt3 --> the3[the]
  nn3 --> telescope[telescope]

```

```

Parse =

```

```

graph TD
  s --> np1[np]
  s --> vp1[vp]
  np1 --> dt1[dt]
  np1 --> nn1[nn]
  dt1 --> the1[the]
  nn1 --> boy[boy]
  vp1 --> vbd[vbd]
  vp1 --> np2[np]
  vbd --> see[see]
  vbd --> ed[ed]
  np2 --> np3[np]
  np2 --> pp[pp]
  np3 --> dt3[dt]
  np3 --> nn3[nn]
  dt3 --> the3[the]
  nn3 --> man[man]
  pp --> in[in]
  pp --> np4[np]
  in --> with[with]
  np4 --> dt4[dt]
  np4 --> nn4[nn]
  dt4 --> the4[the]
  nn4 --> telescope[telescope]

```

Homework 6

- Hint #1:

- consider the case when there are multiple base rules for x

- $x(x(X, y)) \rightarrow x(X), [y]$.

- $x(x(z)) \rightarrow [z]$.

- $x(x(w)) \rightarrow [w]$.

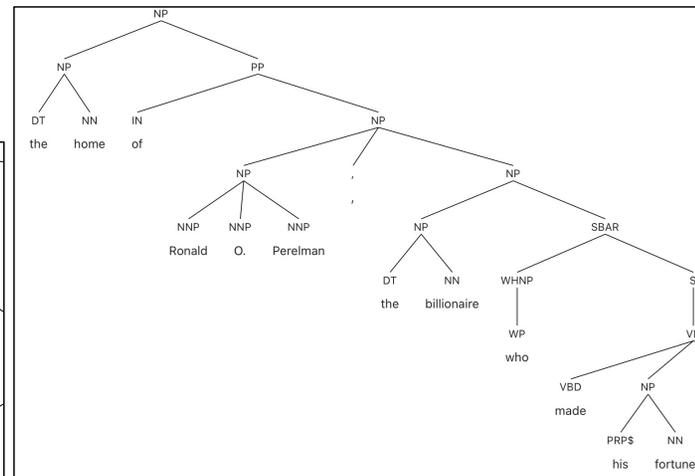
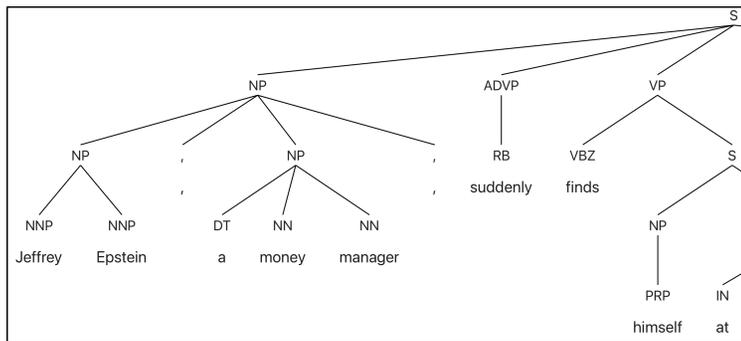
- Hint #2:

- w must be a fresh nonterminal, i.e. cannot be shared between the NP and VP recursions. Why?

Homework 6

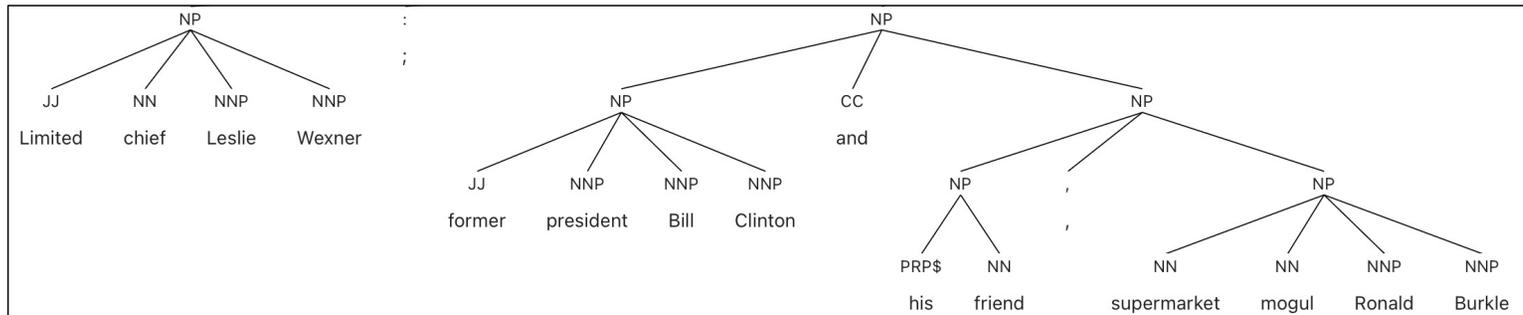
- Question 2: with *appositives*, we also get a left recursive analysis.
- Non-restrictive (*set off by commas*):
 - NP, NP, *Jeffrey Epstein, a money manager, Ronald O. Perelman, the billionaire* (source: NYTimes)

- Berkeley Neural Parser:
parser.kitaev.io



Homework 6

- **Aside:** there's another kind of apposition, but not left recursive (according to the *Berkeley Neural Parser*):



Homework 6

- Question 2: add the comma-separated kind of appositives to your grammar.
 - Part 1: give the left recursive rule.
 - Part 2: apply the transformation (*to eliminate left recursion*).
- Show how you can parse:
 - the boy , a student , saw the man
 - the boy , a student , saw the man , the astronomer ,
- Note:
 - comma needs to be quoted in the input list or grammar rule: [' , ']
 - `s(Parse, [the, boy, ' , ', a, student, ' , ', saw, the, man], [])`.

Homework 6

- Question 3: *no need to implement this*, i.e. don't worry about it, but how can you eliminate the superfluous last comma in Question 2?
 - *the boy , a student , saw the man , the astronomer ,
 - the boy , a student , saw the man , the astronomer
- **Hint:** is it context-free?

Homework 6

- Question 4: can your grammar handle both of these?
 - the boy , a student , saw the man with the telescope
 - the boy , a student , saw the man , the astronomer , with the telescope
- If not, explain why, then modify your grammar.
- If yes, explain why it can.

Homework 6

- Submit to sandiway@arizona.edu
- **SUBJECT:** 581 Homework 6 *YOUR NAME*
- One PDF file (for grading)
 - include your grammar code and SWI-Prolog screenshots in your answer
- Attach (if I need to run your code):
 - source code for your grammar
- Deadline:
 - midnight Monday: **no lecture next Monday** (*I'm away*)
 - we will review the homework next Wednesday