# LING 364: Introduction to Formal Semantics 

Lecture 5<br>January 26th

## Administrivia

- Reminder:
- Homework 1 due on tonight (midnight deadline)
- questions? ask now
- Reading Assignment
- Chapter 2: Putting a Meaning Together from Pieces


## Last Time

- Translating English into logical meaning

Mary is a student
who is a student?


student(mary).

?- student(X).

## Last Time

- Goal:
- formalize language to the degree we can have systems that can understand and answer questions wrt. possible worlds
- demo
- |: john is a student.
- student(john).
- |: mary is a student.
- student(mary).
- |: mary is a baseball fan.
- baseball_fan(mary).
- |: who is a student and not a baseball fan?
- john.
- | ?- go.
- $\mid$ : who is a student and a baseball fan?
- mary.
to do this we have to be able to
(1) parse, and
(2) assign meaning to the English input


## Last Time

## - Syntax:

- A formal grammar enables us to logically break down a sentence into its constituent parts


X-bar phrase structure subject: [12 [NP john] 11] VP: is a student copula: is
complement of VP:
$\left[_{N P}\left[\begin{array}{ll}\text { DET }\end{array} a\right]_{N 1}\right.$ student] $]$ (predicate NP)

## Syntactic Structure

- A formal grammar enables us to logically break down a sentence into its constituent parts


X-bar phrase structure
specifier of CP: [CP [NP who] C1 ]
head of CP: C: auxiliary verb is subject: [12 ${ }_{\text {NP }}$ trace] 11 ]
subject is coindexed [1] with specifier of CP
VP: [y trace] a student
verb (trace) is coindexed [2] with is complement of VP:
$\left[_{\mathrm{NP}} \text { [DET } \mathrm{a}\right]_{\mathrm{N} 1}$ student]]

## Phrase Structure Rules



- Simple rules:
- SBar $\rightarrow$ S subject
- $S \rightarrow$ NPVP
- $\mathrm{VP} \rightarrow \mathrm{VNP} \quad$ object
- $V \rightarrow$ is
- NP $\rightarrow$ DET $N$
- NP $\rightarrow$ ProperNoun
- ProperNoun $\rightarrow$ John
- DET $\rightarrow$ a
- $N \rightarrow$ student


## Phrase Structure Rules

- John is a [pred student]
- John [pred likes] Mary
- John is [pred happy]
- which is the predicate?
- V (main verb: likes)
- $\mathrm{V}_{\text {aux }}$ is (copula carries little meaning)
- complement of copula is the predicate
- Note:
- gotta be careful
- John is the student
- Simple rules:
- SBar $\rightarrow$ S subject
- $S \rightarrow$ NP VP
- $\mathrm{VP} \rightarrow \mathrm{V} \mathrm{NP}$. object
- $V \rightarrow$ is
- NP $\rightarrow$ DET N
- NP $\rightarrow$ ProperNoun
- ProperNoun $\rightarrow$ John
- DET $\rightarrow$ a
- $\mathrm{N} \rightarrow$ student


## Phrase Structure Rules

- Rules:
- SBar $\rightarrow$ WhNoun Aux S
- WhNoun $\rightarrow$ who
- Aux $\rightarrow$ is subject
- $S \rightarrow$ NPtrace VP empty
- NPtrace $-\varepsilon$
- VP $\rightarrow$ Vtrace NP
- Vtrace $\rightarrow \varepsilon$
- NP $\rightarrow$ DET N
- DET $\rightarrow$ a
- $\mathrm{N} \rightarrow$ student
plus associations by coindexation between traces and contentful items


## Today's Topics

1. What is a formal grammar?
2. Prolog's notation for formal grammars

- Definite Clause Grammars

3. Discussion of Putting a Meaning Together from Pieces
4. Short Quiz

## What is a formal grammar?

- example


NP = Noun Phrase
VP = Verb Phrase

- example
- Sentence $\rightarrow$ NP VP
- VP $\rightarrow$ Verb NP
- Verb $\rightarrow$ took
- NP $\rightarrow$ the man
- NP $\rightarrow$ the book
- production (or grammar) rule format
- LHS $\rightarrow$ RHS
- LHS = Left Hand Side
- $\rightarrow \quad=$ "expands to" or "rewrites to"
- RHS = Right Hand Side


## What is a formal grammar?

- example
- Sentence $\rightarrow$ NP VP
- VP $\rightarrow$ Verb NP
- Verb $\rightarrow$ took
- NP $\rightarrow$ the man
- NP $\rightarrow$ the book
derivation
- top-down (one of many)

1. Sentence
2. NP VP
3. NP Verb NP
4. NP took NP
5. the man took NP
6. the man took the book


- derivation
- top-down (alternative)

1. Sentence
2. NP VP
3. the man VP
4. the man Verb NP
5. the man took NP
6. the man took the book

## What is a formal grammar?

- example
- Sentence $\rightarrow$ NP VP
- VP $\rightarrow$ Verb NP
- Verb $\rightarrow$ took
- NP $\rightarrow$ the man
- NP $\rightarrow$ the book
derivation
- bottom-up (one of many)

1. the man took the book
2. NP took the book
3. NP Verb the book
4. NP Verb NP
5. NP VP
6. Sentence


- derivation
- bottom-up (alternative)

1. the man took the book
2. the man took NP
3. the man Verb NP
4. the man $V P$
5. NP VP
6. Sentence

## What is a formal grammar?

- example
- Sentence $\rightarrow$ NP VP
- VP $\rightarrow$ Verb NP
- Verb $\rightarrow$ took
- NP $\rightarrow$ the man

- this grammar can generate more than one sentence
- examples
- the man took the book
- \#the book took the man
\# = semantically odd
- other sentences?
- add new rule
- $\quad$ Verb $\rightarrow$ bought
- examples
- the man took the book
- the man bought the book
- \#the book took the man
\# = semantically odd
- \#the book bought the man


## What is a formal grammar?

- example
- Sentence $\rightarrow$ NP VP
- VP $\rightarrow$ Verb NP
- Verb $\rightarrow$ took
- NP $\rightarrow$ the man
- NP $\rightarrow$ the book

- formally: a grammar contains the following 4 things
- <N,T,P,S>
- a set of non-terminal symbols (N)
- a set of terminal symbols (T)
- production rules $(P)$ of the form
- a designated start symbol (S)
- example
- Non-terminals: $\quad$ SSentence,VP,NP,Verb\}
- Terminals: \{the,man,book,took\}
- Start symbol: Sentence
- Production rules: set of LHS $\rightarrow$ RHS rules


## Grammar Rules

- Good news!
- Prolog supports grammar rules
- it knows how to interpret them (directly)
- it can use grammar rules supplied by the user to construct a derivation automatically


## Prolog Grammar Rules

- Prolog's version of grammar rules:
- Definite Clause Grammar (DCG)
- Prolog's format
- terminals and non-terminal symbols begin with lowercase letters
- e.g. sentence, vp, np, book, took
- Note: variables begin with an uppercase letter (or underscore)
- -->
- is the rewrite symbol
- terminals are enclosed in square brackets to distinguish them from non-terminals (list notation)
- e.g. [the], [book], [took]
- comma (, ) is the concatenation symbol
- semicolon (;) is the disjunction symbol
- a period (.) is required at the end of all DCG rules


## Prolog Grammar Rules

- example
- Sentence $\rightarrow$ NP VP
- VP $\rightarrow$ Verb NP
- Verb $\rightarrow$ took
- NP $\rightarrow$ the man

- Prolog DCG version

```
- sentence --> np, vp.
- vp --> verb, np.
- verb --> [took].
- np --> [the], [man].
- np --> [the], [book].
```

- Important Note
- don't enter these rules into the database using assert/1.
- Use a file.


## Prolog Grammar Rules

- example
- sentence --> np, vp.
- vp --> verb, np.
- verb --> [took].
- np --> [the], [man].
- np --> [the], [book].

query:
- ?- sentence(S,[]).
- $\quad S=$ sentence (as a list)
- [] = empty list
- i.e. call the start symbol as a predicate and
- supply two arguments, a list and an empty list


## Prolog Grammar Rules

- example
- sentence --> np, vp.
- vp --> verb, np.
- verb --> [took].
- np --> [the], [man].
- np --> [the], [book].

example queries
- ?- sentence([the,man,took, the,book],[]).
- Yes
- "the man took the book" is a member of the language generated by the grammar
- ?- sentence([man,took,the,book], []).
- No
- "man took the book" is not in the grammar
- "man took the book" is not generated by the grammar


## Prolog Grammar Rules

- example
- sentence --> np, vp.
- vp --> verb, np.
- verb --> [took].
- np --> [the], [man].
- np --> [the], [book].

other queries
- ?- sentence([the, man, took, X, book], []).
- $\mathrm{X}=$ the
- ?- sentence (S, []).
- $S=[$ the, man, took, the, man] ;
- $S=[$ the, man, took, the, book] ;
- $S=[$ the, book, took, the, man] ;
- $S=[$ the, book, took, the, book] ;
- $\quad \mathrm{NO}$


## Prolog Grammar Rules

- example
- sentence --> np, vp.
- vp --> verb, np.
- verb --> [took].
- np --> [the], [man].
- np --> [the], [book].
notes

$$
\begin{aligned}
& -\quad n p-->[\text { the, man }] . \\
& -\quad n p-->[\text { the, book }] .
\end{aligned}
$$



OK
OK
more grammar
det $=$ determiner

- np --> det, [man].
- np --> det, [book].
- det --> [the].
- det --> [a].


## Prolog Grammar Rules

- example
- sentence --> np, vp.
- vp --> verb, np.
- verb --> [took].
- np --> det, [man].
- np --> det, [book].
- det --> [the].
- det --> [a].



## query

- ?- sentence (S,[]).
- generates 16 different answers for S
- 2 choices for det
a, the
- 2 choices for head noun
- total of 4 different choices for NP
- 2 choices for NP
man, book
(al (the)) ((man) | (book))
as subject, as object
- total $=4^{2}=16$


## Prolog Grammar Rules

- example
- sentence --> np, vp.
- vp --> verb, np.
- verb --> [took].
- np --> det, [man].
- np --> det, [book].
- det --> [the].

- det --> [a].

```
query
- ?- sentence([the,man,took|L],[]).
- L = [the, man] ;
- L = [a, man] ;
- L = [the, book] ;
- L = [a, book] ;
- No
```


## Prolog Grammar Rules

- example
- sentence --> np, vp.
- vp --> verb, np.
- verb --> [took].
- np --> det, [man].
- np --> det, [book].
- det --> [the].

- det --> [a].


## query

- ?- sentence([X,man,took,X,book],[]).
- X $=$ the ;
- $\mathrm{X}=\mathrm{a}$;
- $\quad \mathrm{No}$


## 2 choices

## Putting a Meaning Together from Pieces

- Chapter ties into what we've been doing:
-driven by syntax
- we're going to compute meaning in parts


# Putting a Meaning Together from Pieces 

- 2.2 Incomplete Propositions
- Shelby barks barks(shelby).
- barks
???


# Putting a Meaning Together from Pieces 

- 2.2 Incomplete Propositions
- Shelby barks barks(shelby).
- barks barks $(\mathrm{X})$.
- predicate
- = unsaturated proposition


## Putting a Meaning Together from Pieces

- 2.3 Saturation
- Shelby barks
- barks
- Shelby

barks(shelby).<br>barks(X).<br>shelby

- predication:
- relation between predicate barks(X) and its subject shelby
- barks is "predicated of" shelby
- i.e. barks $(X)$ and $X=$ shelby


## Putting a Meaning Together from Pieces

- 2.4 Compositionality
- (discrete) infinity and creativity of language (new phrases)
- Principle of Compositionality
- Meaning(Phrase) = composition of Meaning(SubPart ${ }_{1}$ ), Meaning(SubPart ${ }_{2}$ ) and so on...
- Example: Shelby barks


## Putting a Meaning Together from Pieces

- 2.5 Syntax and Semantics
- Principle of Compositionality can be realized in different ways
- Theories of Meaning:
- rule-by-rule theories
- interpretive theories
- Example:
- What did John sit on?
- John sat on what
(+ Wh-phrase movement)


## A different kind of example

- Think about the meaning of any in:

1. any dog can do that trick
2. I didn't see any dog
3. *I saw any dog
how many meanings does any have?
do you see any potential problems for rule-by-rule theories?

## A different kind of example

- Think about the meaning of any in:

1. any dog can do that trick
2. I didn't see any dog
3. *I saw any dog
how many meanings does any have?
a) "free choice" any
b) negative polarity item (NPI) any

## Quiz

- [5pts]
- give meaning fragments for:
- John
- likes Mary
- likes
- in "John likes Mary" corresponds to likes(john,mary).
- give syntactic structures for:
- who is a student and not a baseball fan?
- who is not a baseball fan or a student?

